

GCSE Mathematics

Practice Tests: Set 3

Paper 1H (Non-calculator)

Time: 1 hour 30 minutes

You should have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator.

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided – *there may be more space than you need.*
- **Calculators may not be used.**
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must **show all your working out.**



Information

- The total mark for this paper is 80
- The marks for **each** question are shown in brackets – *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

Answer ALL questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1. The equation of a straight line is $y = 4x + 7$

(a) Write down the gradient of the line.

$$y = mx + c$$

↑
↑
 gradient y-intercept

4
.....
(1)

(b) Write down the y-intercept of the line.

7
.....
(1)

(Total 2 mark)

2. Work out $3\frac{1}{8} - 1\frac{2}{3}$

Mixed Number Operations

$$3\frac{1}{8} = \frac{25}{8}$$

$$1\frac{2}{3} = \frac{5}{3}$$

$$\text{LCM} = 24$$

$$\begin{aligned}
 &3\frac{1}{8} - 1\frac{2}{3} \\
 &= \frac{25}{8} - \frac{5}{3} \\
 &= \frac{75}{24} - \frac{40}{24} \\
 &= \frac{35}{24}
 \end{aligned}$$

$\frac{35}{24}$

 (Total 3 marks)

3. Here are the ingredients needed to make 8 shortbread biscuits.

Shortbread biscuits makes 8 biscuits 120 g butter 60 g caster sugar 180 g flour

Tariq is going to make some shortbread biscuits.
He has the following ingredients

330 g butter 200 g caster sugar 450 g flour

Work out the greatest number of shortbread biscuits that Tariq can make with his ingredients.
You must show all your working.

UNITARY
↓

How much ingredient
needed for 1 biscuit?

$$\begin{array}{r} 7.5 \\ 8 \overline{) 60.0} \end{array}$$

Butter: $120g \div 8 = 15g$

Caster: $60g \div 8 = 7.5g$

Flour: $180g \div 8 = 22.5g$

$$\begin{array}{r} 022.5 \\ 8 \overline{) 180.0} \end{array}$$

Could we make 10?

Butter: $15g \times 10 = 150g \checkmark$

Caster: $7.5g \times 10 = 75g \checkmark$ YES

Flour: $22.5g \times 10 = 225g \checkmark$

20?

Butter: $300g \checkmark$

Caster: $150g \checkmark$ YES

Flour: $450g \checkmark$

..... biscuits

Conclusion

We have used all the flour

(Total 3 marks)

\therefore maximum = 20 biscuits

Percentages of an Amount

4. Railtickets and Cheaptrains are two websites selling train tickets.

Each of the websites adds a credit card charge and a booking fee to the ticket price.

Railtickets
Credit card charge: 2.25% of ticket price
Booking fee: 80 pence

Cheaptrains
Credit card charge: 1.5% of ticket price
Booking fee: £1.90

Nadia wants to buy a train ticket.
The ticket price is £60 on each website.
Nadia will pay by credit card.

Will it be cheaper for Nadia to buy the train ticket from Railtickets or from Cheaptrains?

Railtickets

① credit charge

2.25% of £60

1% = £0.60

0.5% = £0.30

0.25% = £0.15 (+)

2% = £1.20

∴ 2.25% = £1.35

② Booking fee

fee = £0.80

Total = £1.35 + £0.80

= £2.15

∴ It is cheaper for Nadia to buy from railtickets! (Total 4 marks)

Cheaptrain's

① credit charge

1.5% of £60

1% = £0.60 (+)

0.5% = £0.30

∴ 1.5% = £0.90

② Booking fee

fee = £1.90

Total = £1.90 + £0.90

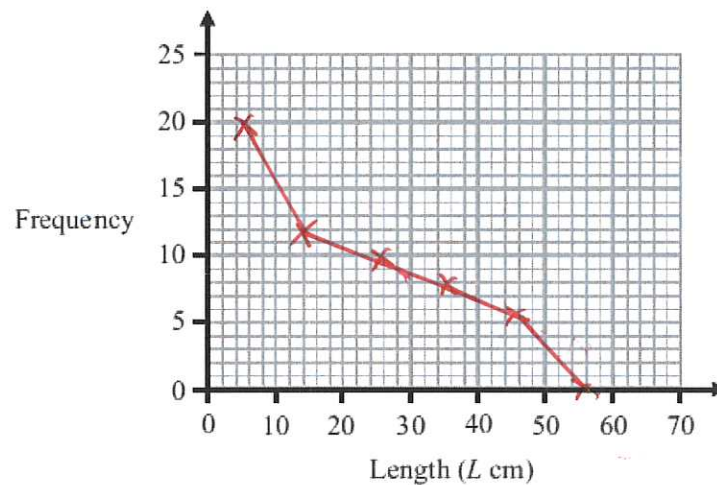
= £2.80

Frequency Polygon

5. The table gives information about the lengths of the branches on a bush.

Length(Lcm)	<i>midpoints!</i>	
		Frequency
$0 \leq L < 10$	<i>5</i>	20
$10 \leq L < 20$	<i>15</i>	12
$20 \leq L < 30$	<i>25</i>	10
$30 \leq L < 40$	<i>35</i>	8
$40 \leq L < 50$	<i>45</i>	6
$50 \leq L < 60$	<i>55</i>	0

- (a) Draw a frequency polygon to show this information.



(2)

- (b) Work out the total number of branches on the bush.

$$\begin{aligned}
 \text{Total frequency} &= 20 + 12 + 10 + 8 + 6 + 0 \\
 &= 32 + 10 + 14 \\
 &= 32 + 24 \\
 &= 56
 \end{aligned}$$

..... *56*

(2)

- (c) Write down the modal class interval.

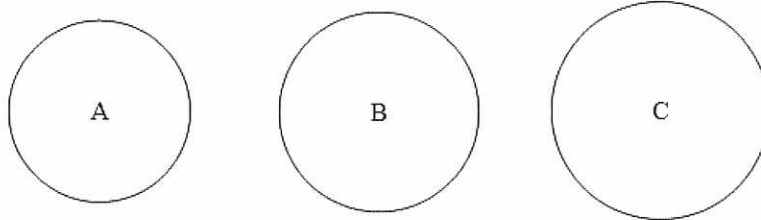
↓
highest frequency

..... *0 ≤ L < 10*

(1)

(Total 5 marks)

6. Here are three circles A, B and C.



Diagrams NOT accurately drawn

The area of circle A is 200 cm^2 .

The area of circle B is 10% larger than the area of circle A.

The area of circle C is 10% larger than the area of circle B.

How much larger is the area of circle C than the area of circle A?

Area B $200 \text{ cm}^2 + 10\% = 220 \text{ cm}^2$

Area C $220 \text{ cm}^2 + 10\% = 242 \text{ cm}^2$

Compare A and C $242 \text{ cm}^2 - 200 \text{ cm}^2 = \underline{\underline{42 \text{ cm}^2 \text{ larger}}}$

(Total 4 marks)

7. (a) Expand and simplify $2(x + 3y) + 4(x - y)$

$$\begin{array}{l} \text{Expand} \\ \text{Collect} \end{array} \left| \begin{array}{l} 2x + 6y + 4x - 4y \\ 6x + 2y \end{array} \right.$$

$$\underline{\hspace{10em} 6x + 2y \hspace{10em}}$$

(2)

- (b) Factorise completely $8p - 12pq$

$$\begin{aligned} & 8p - 12pq \\ &= 4(2p - 3pq) \\ &= 4p(2 - 3q) \end{aligned}$$

$$\underline{\hspace{10em} 4p(2 - 3q) \hspace{10em}}$$

(2)

(Total 4 marks)

8. The diagram shows a triangle.

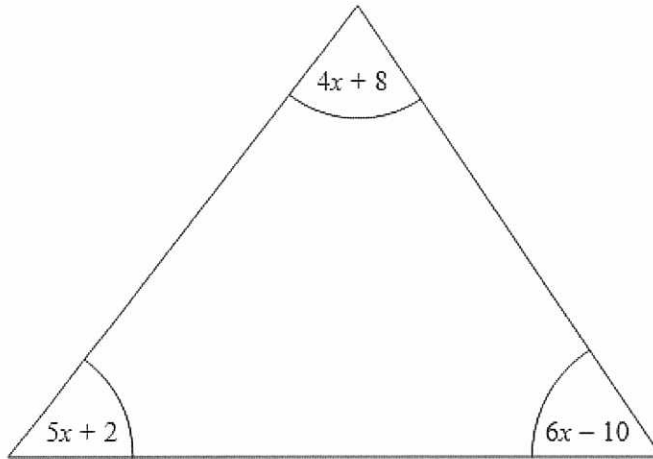


Diagram NOT accurately drawn

All the angles are measured in degrees.

Show that the triangle is isosceles.

$$\frac{12}{15 \mid 180}$$

Angles in a $\Delta = 180^\circ$
collect
($\div 15$)

$$\begin{aligned} 4x + 8 + 5x + 2 + 6x - 10 &= 180 \\ 15x &= 180 \\ x &= 12^\circ \end{aligned}$$

Substitute $x = 12$

$$\begin{aligned} \textcircled{1} \quad 5x + 2 &= 5(12) + 2 \\ &= 60 + 2 = 62^\circ \\ \textcircled{2} \quad 6x - 10 &= 6(12) - 10 \\ &= 72 - 10 = 62^\circ \\ \textcircled{3} \quad 4x + 8 &= 4(12) + 8 \\ &= 48 + 8 = 56^\circ \end{aligned}$$

(Total 5 marks)

Conclusion

The triangle is isosceles since two of the angles are the same. \square .

HCF/LCM

9. (a) Find the Highest Common Factor (HCF) of 30 and 42.

$$\underline{30}: 1, 2, 3, 5, 6, 10, 15, 30$$

$$\underline{42}: 1, 2, 3, 6, 7, 14, 21, 42$$

6

.....
(2)

- (b) Find the Lowest Common Multiple (LCM) of 30 and 45.

$$\underline{30}: 30, 60, 90$$

$$\underline{45}: 45, 90$$

90

.....
(2)

(Total 4 marks)



10.

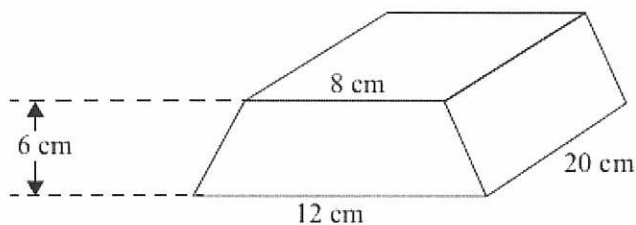


Diagram NOT accurately drawn

The diagram shows a solid prism made from metal.
The cross-section of the prism is a trapezium.

The parallel sides of the trapezium are 8 cm and 12 cm.
The height of the trapezium is 6 cm.
The length of the prism is 20 cm.

The density of the metal is 5 g/cm³.

Calculate the mass of the prism.
Give your answer in kilograms.

front face

Cross-sectional area
 $= \frac{h(a+b)}{2}$

$$A = \frac{6(8+12)}{2}$$
$$= \frac{6(20)}{2} = \frac{120}{2} = 60 \text{ cm}^2$$

$$V = CSA \times L$$

$$V = 60 \text{ cm}^2 \times 20 \text{ cm}$$
$$= 1200 \text{ cm}^3$$

$$m = D \times V$$

$$m = 5 \text{ g/cm}^3 \times 1200 \text{ cm}^3$$

$$m = 6000 \text{ g}$$

$$m = 6 \text{ kg}$$

..... 6 kg

(Total 5 marks)

g to kg conversion

Index Laws

11. (a) Write down the value of 25^0

$$a^0 = 1$$

$$\frac{1}{\dots\dots\dots}$$

(1)

(b) Write down the value of $49^{\frac{1}{2}}$

$$a^{\frac{1}{m}} = \sqrt[m]{a} \quad | \quad 49^{\frac{1}{2}} = 7^{-1}$$

$$a^{-m} = \frac{1}{a^m} \quad | \quad 7^{-1} = \frac{1}{7}$$

$$\frac{1}{7}$$

(1)

(c) Write as a power of 2 $\frac{4 \times 8}{16^3}$

Change of base

$$4 = 2 \times 2 = 2^2$$

$$8 = 2 \times 2 \times 2 = 2^3$$

$$16 = 2 \times 2 \times 2 \times 2 = 2^4$$

$$a^m \times a^n = a^{m+n}$$

$$\frac{4 \times 8}{16^3} = \frac{2^2 \times 2^3}{(2^4)^3}$$

$$= \frac{2^5}{(2^4)^3}$$

$$2^{-7}$$

(3)

(Total 5 marks)

$$(a^m)^n = a^{m \times n}$$

$$= \frac{2^5}{2^{12}}$$

$$\frac{a^m}{a^n} = a^{m-n}$$

$$= \underline{\underline{2^{-7}}}$$

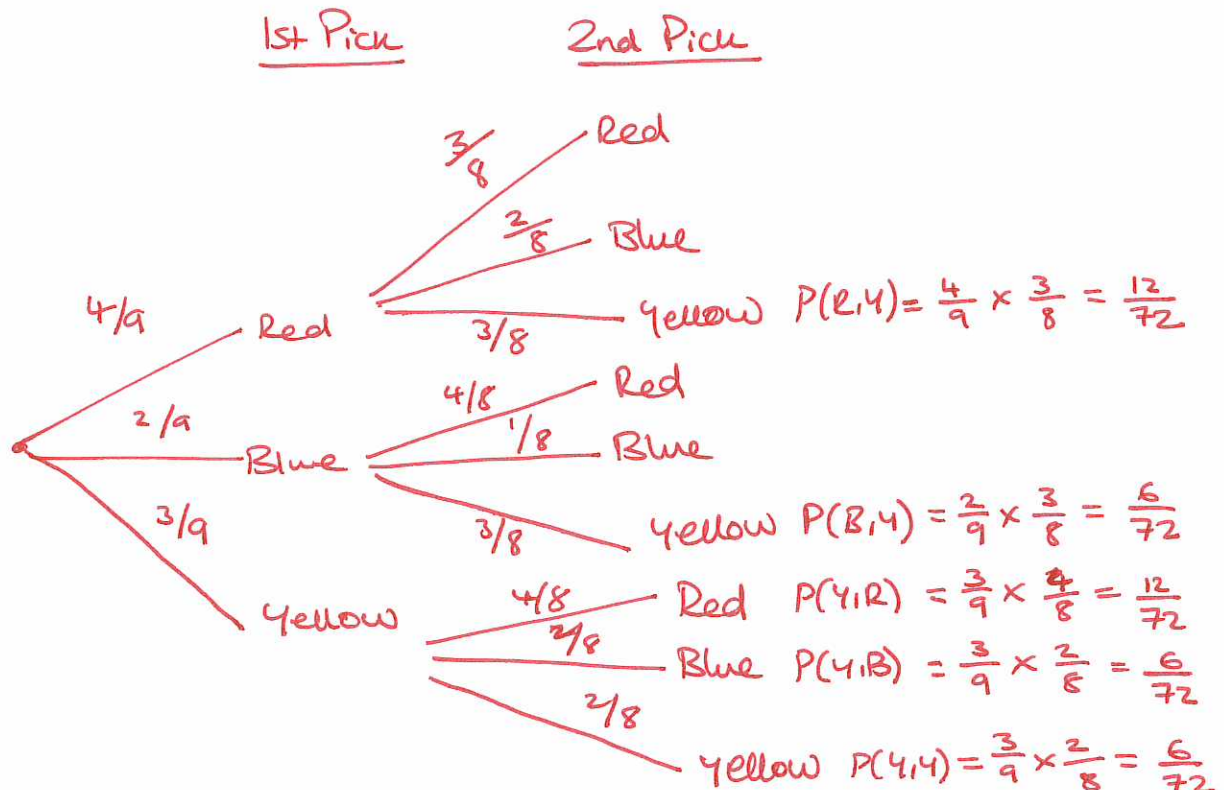
Dependent Probability Trees

12. There are 9 counters in a box.

- 4 of the counters are red.
- 2 of the counters are blue.
- 3 of the counters are yellow.

Pavinder takes at random two counters from the box.

Work out the probability that he takes at least one yellow counter.



$$\begin{aligned}
 P(\text{at least one yellow}) &= P(R,Y) + P(B,Y) + P(Y,R) + P(Y,B) + P(Y,Y) \\
 &= \frac{12+6+12+6+6}{72} = \frac{42}{72} \quad \text{(Total 4 marks)}
 \end{aligned}$$

Simplifying Algebraic Fractions

13. Simplify fully $\frac{2x^2 - 7x + 3}{x^2 - 9}$

$$\begin{array}{l|l}
 \text{factorise top} & (2x - 1)(x - 3) \\
 \text{factorise bottom} & (x + 3)(x - 3) \\
 & = \frac{(2x - 1)(\cancel{x - 3})}{(x + 3)(\cancel{x - 3})} \\
 \text{Simplify} & = \frac{2x - 1}{x + 3}
 \end{array}$$

$$\frac{2x - 1}{x + 3}$$

(Total 3 marks)

14. Work out $(2 + \sqrt{3})(2 - \sqrt{3})$
Give your answer in its simplest form.

Expanding Surds Brackets

$$\begin{array}{l|l}
 \text{expand} & (2 + \sqrt{3})(2 - \sqrt{3}) \\
 & = 4 - 2\sqrt{3} + 2\sqrt{3} - 3 \\
 \sqrt{3}x - \sqrt{3} = -3 \quad \text{collect} & = \underline{\underline{1}}
 \end{array}$$

1

(Total 2 marks)

15.

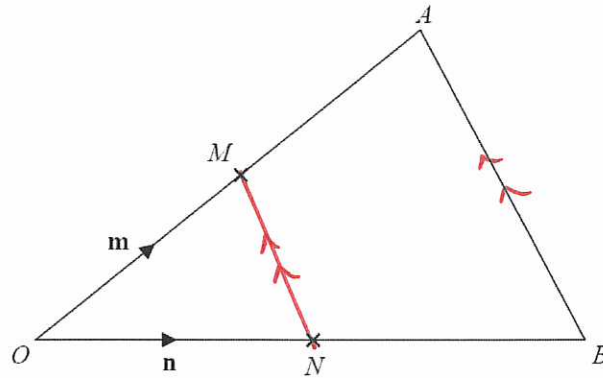


Diagram NOT accurately drawn

OAB is a triangle.
 M is the midpoint of OA .
 N is the midpoint of OB .

$$\vec{OM} = \mathbf{m}$$

$$\vec{ON} = \mathbf{n}$$

Show that AB is parallel to MN .

$$\vec{AB} = -2\mathbf{m} + 2\mathbf{n}$$

$$\vec{MN} = -\mathbf{m} + \mathbf{n}$$

$$\therefore \vec{AB} = 2\vec{MN}$$

Since \vec{AB} is a scalar vector of \vec{MN} , the two ~~lines~~ are parallel. \square

(Total 3 marks)

16.

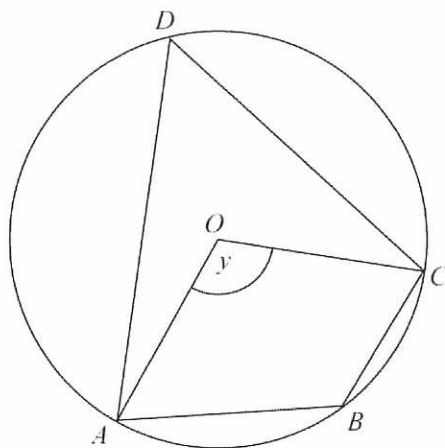


Diagram NOT accurately drawn

A, B, C and D are points on the circumference of a circle, centre O .

Angle $AOC = y$.

Find the size of angle ABC in terms of y .

Give a reason for each stage of your working.

$$\hat{AOC} = \frac{y}{2}$$

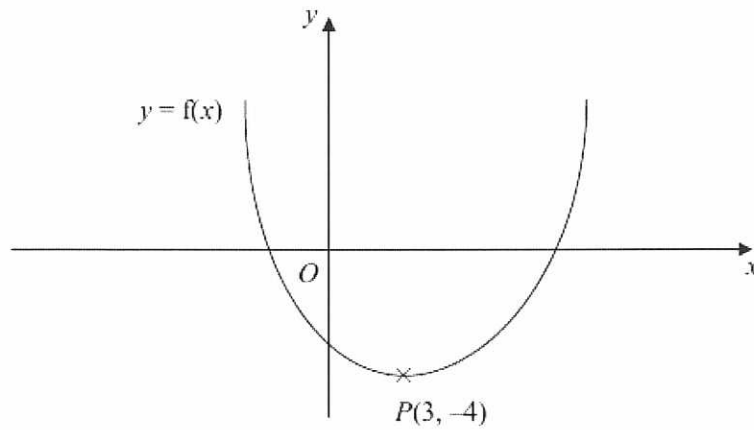
$$\hat{ABC} = \underline{\underline{180 - \frac{y}{2}}}$$

Angle at the circumference is half that at the centre

opposite angles in a cyclic quadrilateral ~~are~~ $= 180^\circ$

(Total 4 marks)

17. This is a sketch of the curve with the equation $y = f(x)$.
The only minimum point of the curve is at $P(3, -4)$.



- (a) Write down the coordinates of the minimum point of the curve with the equation $y = f(x - 2)$.

Translation of $\begin{bmatrix} 2 \\ 0 \end{bmatrix}$

(.....,)
5 -4
(2)

- (b) Write down the coordinates of the minimum point of the curve with the equation $y = f(x + 5) + 6$

Translation of $\begin{bmatrix} -5 \\ 6 \end{bmatrix}$

(.....,)
-2 2
(2)

(Total 4 marks)

18.

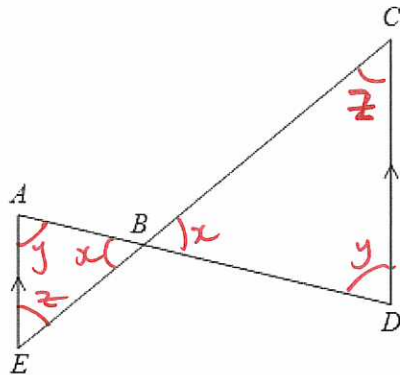


Diagram NOT
accurately drawn

AE is parallel to CD .

ABD and EBC are straight lines.

Prove that triangle ABE is similar to triangle DCB .

Give reasons for each stage of your proof.

$$\hat{A}BE = \hat{C}BD = x^\circ$$

$$\hat{B}AE = \hat{B}DC = y^\circ$$

$$\hat{A}EB = \hat{B}CD = z^\circ$$

All angles are the
same \therefore Similar.

Vertically opposite angles are equal
Alternate angles in parallel lines are equal.
Alternate angles in parallel lines are equal

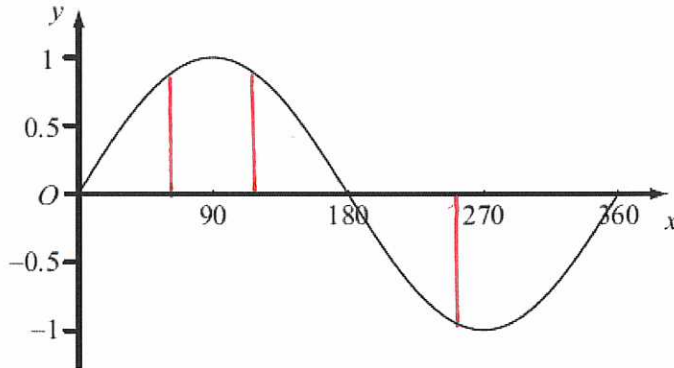
Conclusion:



(Total 4 marks)

Trigonometric Functions

19. The diagram shows a sketch of the curve $y = \sin x^\circ$ for $0 \leq x \leq 360$



The exact value of $\sin 60^\circ = \frac{\sqrt{3}}{2}$

(a) Write down the exact value of

(i) $\sin 120^\circ$,

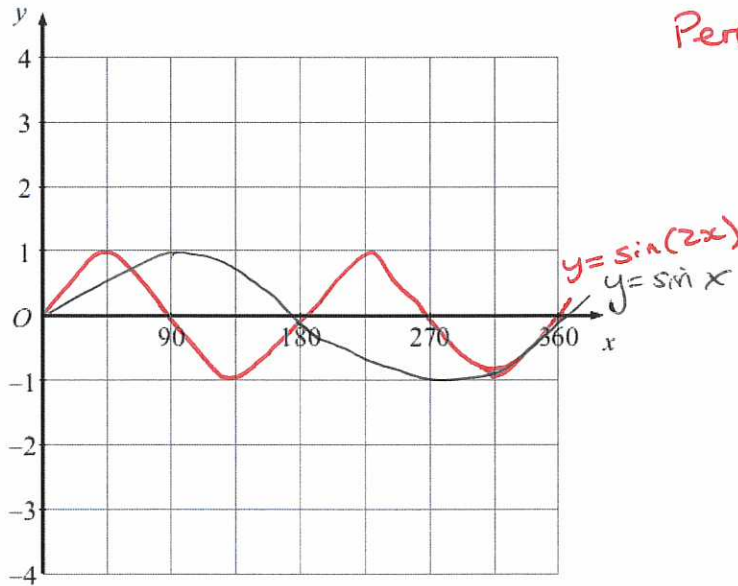
(ii) $\sin 240^\circ$.

$$\frac{\sqrt{3}}{2}$$

$$-\frac{\sqrt{3}}{2}$$

(2)

(b) On the grid below, sketch the graph of $y = \sin 2x^\circ$ for $0 \leq x \leq 360$



Period has been doubled.

(2)

(Total 4 marks)

Algebraic Proof

20. Prove algebraically that the difference between the squares of any two consecutive integers is equal to the sum of these two integers.

n and $n+1$

Squares: $(n+1)^2$ and n^2

expand

$$(n+1)^2 - (n)^2$$

$$(n+1)(n+1) - n^2$$

$$n^2 + n + n + 1 - n^2$$

collect

$$n + n + 1$$

$$\underline{\underline{2n+1}}$$

Conclusion:

$2n+1$ is the sum of $n+1+n$ ($=2n+1$) \square .

(Total 4 marks)

Completing The Square

- 21 Sketch the graph of $f(x) = -x^2 - 3x + 5$, showing the coordinates of the turning point and the coordinates of any intercepts with the coordinate axes.

factorise to make it easier

complete the square

Simplify

expand

Turning Point

Solve by setting $y=0$

$$\left(-\frac{29}{4}\right)$$

$$(x-1)$$

$\sqrt{\text{ANS}}$

$$\left(-\frac{3}{2}\right)$$

ROOTS :

$$y = -x^2 - 3x + 5$$

$$y = -(x^2 + 3x - 5)$$

$$y = -\left[\left(x + \frac{3}{2}\right)^2 - \frac{9}{4} - 5\right]$$

$$y = -\left[\left(x + \frac{3}{2}\right)^2 - \frac{29}{4}\right]$$

$$y = -\left(x + \frac{3}{2}\right)^2 + \frac{29}{4}$$

$$\left(-\frac{3}{2}, \frac{29}{4}\right)$$

$$0 = -\left(x + \frac{3}{2}\right)^2 + \frac{29}{4}$$

$$-\frac{29}{4} = -\left(x + \frac{3}{2}\right)^2$$

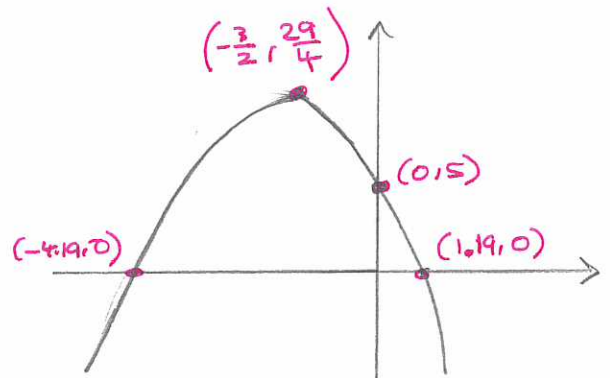
$$\frac{29}{4} = \left(x + \frac{3}{2}\right)^2$$

$$\pm\sqrt{\frac{29}{4}} = x + \frac{3}{2}$$

$$\pm\sqrt{\frac{29}{4}} - \frac{3}{2} = x$$

$$1.19 = x +$$

$$-4.19 = x -$$



(Total 4 mark)

TOTAL FOR PAPER IS 80 MARKS