# Higher tier unit 12 check in test

# Calculator

Q1. Identify the two congruent triangles.



Q2. The diagram shows two rectangles.



The rectangles are similar. Work out the value of *w*.

Q3. Quadrilaterals *ABCD* and *LMNP* are mathematically similar.



Work out the length of *LP*.



Q5. *ABCD* and *AEFG* are mathematically similar trapeziums.



Diagram NOT accurately drawn

Trapezium *AEFG* has an area of  $36 \text{ cm}^2$ . Work out the area of the shaded region.

#### [Q6–7 linked]

Q6. The diagram shows two similar solids, A and B.



Solid A has a volume of 80 cm<sup>3</sup>.

Write the relationship between the volume of shape A and the volume of shape B as a ratio in its simplest form

- Q7. Work out the volume of solid B in question 7.
- Q8. Prisms A and B are similar.



The surface area of A is  $135 \text{ cm}^2$ . The surface area of B is 240 cm<sup>2</sup>. The volume of A is 864 cm<sup>3</sup>.

Work out the volume of prism B.

Q9. A frustrum is made by removing a small cone from a similar large cone.



Diagram NOT accurately drawn

The height of the small cone is 20 cm. The height of the large cone is 40 cm. The diameter of the base of the large cone is 30 cm.

Work out the volume of the frustrum. Give your answer correct to 3 significant figures.



In the diagram,

*ADE* is a right-angled triangle, *ABCD* and *AEFG* are squares.

Prove that triangle *ABE* is congruent to triangle *ADG*.

Q10.

# Topics listed in objectives

- Understand and use SSS, SAS, ASA and RHS conditions to prove the congruence of triangles using formal arguments, and to verify standard ruler and pair of compasses constructions;
- Solve angle problems by first proving congruence;
- Understand similarity of triangles and of other plane shapes, and use this to make geometric inferences;
- Prove that two shapes are similar by showing that all corresponding angles are equal in size and/or lengths of sides are in the same ratio/one is an enlargement of the other, giving the scale factor;
- Use formal geometric proof for the similarity of two given triangles;
- Understand the effect of enlargement on angles, perimeter, area and volume of shapes and solids;
- Identify the scale factor of an enlargement of a similar shape as the ratio of the lengths of two corresponding sides, using integer or fraction scale factors;
- Write the lengths, areas and volumes of two shapes as ratios in their simplest form;
- Find missing lengths, areas and volumes in similar 3D solids;
- Know the relationships between linear, area and volume scale factors of mathematically similar shapes and solids;
- Use the relationship between enlargement and areas and volumes of simple shapes and solids;
- Solve problems involving frustums of cones where you have to find missing lengths first using similar triangles.

# Answers

- Q1. A and D
- Q2. w = 21 cm
- Q3. 7.5 cm
- Q4. C
- Q5. 45 cm<sup>2</sup>
- Q6. 1:8
- Q7.  $640 \text{ cm}^3$
- Q8.  $2048 \,\mathrm{cm}^3$
- Q9.  $8250 \text{ cm}^3$
- Q10. AD = AB and AE = AG; angle EAB = angle DAG, so SAS